# Microstructures and microwave dielectric properties of $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$ solid solutions

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**Abstract:**  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  (x=0.02, 0.04, 0.06, 0.08, 0.1) solid solutions were prepared by the conventional solid-state reaction process. It was found that  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics are fully composed of  $BaSm_2Ti_4O_{12}$  and  $BaNd_2Ti_5O_{14}$  phases for all the compositions. The increasing x value  $(0.02 \le x \le 0.1)$  in  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics can not only obtain high  $Q \times f$  value but also effectively enhance the permittivity ( $\varepsilon_r$ ). The  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic with x=0.08, sintered at 1440 °C for 4 h, shows excellent microwave dielectric properties of permittivity ( $\varepsilon_r$ )  $\approx 93.19$ , quality factor  $(Q \times f) \approx 9770.14$  GHz (at 3.415 GHz), and almost near-zero temperature coefficient of resonant frequency ( $\tau_f$ )  $\approx +4.56$  ppm/°C.

Keywords: tungsten bronze type; high permittivity; microwave dielectric properties

### 1 Introduction

As is well-known, the microwave dielectric ceramic materials with high quality factor  $(Q \times f)$  and high permittivity  $(\varepsilon_r)$  have been developed for applications in satellite positioning, navigation, and wireless communication. At present, microwave telecommunication and satellite broadcasting has become one of the fastest developing segments in the communications and electronics industry. Meanwhile, the widespread usage of several wireless systems has required dielectric components that are low-cost, lightweight, small, multifunctional, and highly reliable

In early time, Bolton [2] has reported one unknown BaO–Nd<sub>2</sub>O<sub>3</sub>–TiO<sub>2</sub> ternary compound, which has a high relative permittivity ( $\varepsilon_r$ ) and a low temperature coefficient of resonant frequency ( $\tau_f$ ). Later, Ohsato and co-workers [3,4] have done extensive work on the preparation, characterization, and structure and property investigation of tungsten bronze type materials. In addition, Valant *et al.* [5] and Varfolomeeva and Miranov [6] displayed Ba<sub>3.75</sub>Nd<sub>9.5</sub>Ti<sub>18</sub>O<sub>54</sub> and BaNd<sub>2</sub>Ti<sub>4</sub>O<sub>12</sub> compounds as specific compositions of the solid solution phase Ba<sub>6-3x</sub>Nd<sub>8+2x</sub>Ti<sub>18</sub>O<sub>54</sub> (0  $\leq$ 

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to reduce the device size. In addition, high dielectric constant, high quality factor, and near-zero temperature coefficient of resonant frequency are three key properties required for microwave resonator materials [1].

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 $x \le 0.75$ ). According to several authors [7,8],  $Ba_{6-3x}Ln_{8+2x}Ti_{18}O_{54}$  ceramics based on Gd, Sm, and Nd have high quality factors  $(Q \times f)$  up to 14,000 GHz, and the La-based ceramics have the highest relative permittivity ( $\varepsilon_r = 104$ ). Ohsato *et al.* [9] have also established a relation between the microwave dielectric properties of  $Ba_{6-3x}Sm_{8+2x}Ti_{18}O_{54}$  (0.3  $\le x \le 0.7$ ) solid solution and the crystal structure. It shows that substitution of  $Sm^{3+}$  for  $Ba^{2+}$  in the large cation sites results in the creation of vacancies and crystal distortion, indicating that the shrinkage of the  $TiO_6$  octahedral site plays an important role for the improvement of microwave dielectric properties.

The microwave dielectric properties of  $Ba_{6-3x}Ln_{8+2x}$  $Ti_{18}O_{54}$  (Ln = La, Nd, Sm) materials have been studied sufficiently due to their high permittivity. However, the restriction of  $Q \times f$  and  $\tau_f$  values impedes their commercial application [10-13]. Furthermore, there are a large number of active atoms at the solid solution surface, which has a high interfacial dielectric loss induced by interface polarization [14,15]. In order to resolve these problems, much work has been done to improve the  $Q \times f$  and  $\tau_f$  values. Many attentions have been paid to improve the microwave dielectric properties by substitution of Ba<sup>2+</sup> and Nd<sup>3+</sup> ions using  $Sr^{2+}$  and  $Y^{3+}$  ions, as well as adding NdAlO<sub>3</sub> or Al<sub>2</sub>O<sub>3</sub>. As can be seen from Table 1, all of them find that the substitution of ions can significantly enhance  $Q \times f$  and reduce  $\tau_f$  [16–19].

 $Ba_{6-3x}Ln_{8+2x}Ti_{18}O_{54}$  (Ln=La, Nd, Sm) has been reported to possess high permittivity ( $\varepsilon_r$ ) and quality factor ( $Q \times f$ ) [20–24]. The aim of our present work is to improve the microwave dielectric properties of ( $Ba_{1-x}Sr_x$ )<sub>4</sub>( $Sm_{0.4}Nd_{0.6}$ )<sub>28/3</sub> $Ti_{18}O_{54}$  by substituting the  $Sr^{2+}$  ions. The effects of substitution of  $Sr^{2+}$  ions on the microstructures and microwave dielectric properties of ( $Ba_{1-x}Sr_x$ )<sub>4</sub>( $Sm_{0.4}Nd_{0.6}$ )<sub>28/3</sub> $Ti_{18}O_{54}$  ceramics are investigated systematically.

Table 1 Dielectric properties of  $Ba_{6-3x}Ln_{8+2x}Ti_{18}O_{54}$  ceramics

| Traditional sample  | $\mathcal{E}_{\mathrm{r}}$ | $Q \times f(GHz)$ | $\tau_f \; (\mathrm{ppm/\mathbb{C}})$ |
|---|----------------------------|-------------------|---------------------------------------|
| $\overline{Ba_{6-3x}(Sm_{0.2}Nd_{0.8})_{8+2x}Ti_{18}O_{54}\ (x=2/3)}$ | 80.80                      | 8100              | +35.5                                 |
| $Ba_{6-3x}(Sm_{0.9}Bi_{0.1})_{8+2x}Ti_{18}O_{54} (x = 2/3)$           | 84.10                      | 7840              | -21.0                                 |
| $(Ba_{1-x}Sr_x)_{4.2}Sm_{9.2}Ti_{18}O_{54} (x = 0.04)$                | 80.60                      | 9590              | -11.9                                 |
| $(Ba_{0.6}Pb_{0.4})_{6-3x}La_{8+2x}Ti_{18}O_{54} (x = 1.5)$           | 95.00                      | 6000              | +200.0                                |
| $Ba_{6-3x}(Sm_{0.9}La_{0.1})_{8+2x}Ti_{18}O_{54} (x = 2/3)$           | 84.00                      | 9000              | +4.2                                  |
| $(Ba_{0.8}Sr_{0.2})_{6-3x}Nd_{8+2x}Ti_{18}O_{54} (x = 0.2)$           | 95.00                      | 5500              | +125.0                                |
| $(Ba_{0.7}Sr_{0.3})_{4.8}(Sm_{0.7}La_{0.3})_{8.8}Ti_{18}O_{54}$       | 98.77                      | 5184              | +10.9                                 |

## 2 Experimental procedure

The raw materials were high-purity oxide powders: BaCO<sub>3</sub> (99.8%, Guo-Yao Co. Ltd., Shanghai, China), SrCO<sub>3</sub> (99.8%, Guo-Yao Co. Ltd., Shanghai, China), Nd<sub>2</sub>O<sub>3</sub> (99.8%, Guo-Yao Co. Ltd., Shanghai, China), Sm<sub>2</sub>O<sub>3</sub> (99.8%, Guo-Yao Co. Ltd., Shanghai, China), and TiO<sub>2</sub> (99%, Guo-Yao Co. Ltd., Shanghai, China), and they were mixed according to the desired stoichiometry  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  (x = 0.02, 0.04, 0.06, 0.08, 0.1). The mixed powders were ground in distilled water for 24 h in a ball mill with ZrO₂ balls, then dried and calcined at 1100 °C for 4 h in air. The calcined powders were ground into fine powders, and then the fine powders were pressed into pellets with dimensions of 12 mm in diameter and 5-6 mm in thickness under a pressure of 150 MPa, with 5 wt% PVA as binder. These pellets were sintered at temperatures of 1400-1460 °C for 4 h in air.

The apparent density ( $\rho_a$ ) of sintered ceramics was measured by the Archimedes method, and the bulk density ( $\rho_b$ ) was evaluated from the dimensions and weight. Correspondingly, the relative density ( $\rho_r$ ) was calculated with the following formula:

$$\rho_{\rm r} = \frac{\rho_{\rm a}}{\rho_{\rm b}} \times 100\% \tag{1}$$

The crystalline phases of the sintered ceramics were identified by X-ray diffraction (XRD) using Cu Ka radiation (Rigaku D/MAX-2400 X-ray diffractometer, Tokyo, Japan). Surface topologies of the ceramics were observed by scanning electron microscopy (SEM; JSM-6460, JEOL, Tokyo, Japan). Meanwhile, in order to investigate the effect of Sr<sup>2+</sup> substitution for Ba<sup>2+</sup>, (x = 0.08)the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$ ceramic was studied by energy-dispersive X-ray spectroscopy (EDX). Microwave dielectric properties of the ceramics were measured by the  $TE_{01\delta}$  shielded cavity method with a network analyzer (8720ES, Agilent, Palo Alto, CA, USA) and a temperature chamber (Delta9023, Delta Design, Poway, CA, USA) in the temperature range of 25-75 °C [25,26]. The temperature coefficient of resonant frequency ( $\tau_{\scriptscriptstyle f}$ ) value was calculated with the following formula [27]:

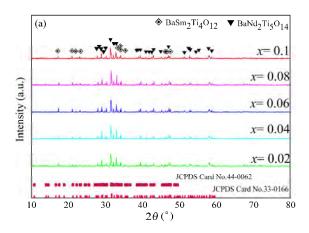
$$\tau_f = \frac{\Delta f_0}{f_0 \Delta T} = \frac{f_{75} - f_{25}}{f_{25} \times 50} \tag{2}$$

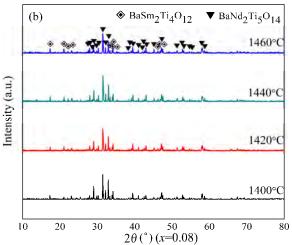
where  $f_{25}$  and  $f_{75}$  were the resonant frequencies at 25 °C and 75 °C, respectively.

## 3 Results and discussion

### 3. 1 Crystalline structures

Figure 1(a) illustrates the room-temperature XRD patterns recorded from  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}$   $Ti_{18}O_{54}$  (x=0.02, 0.04, 0.06, 0.08, 0.1) ceramics sintered at 1440 °C for 4 h. As shown in Fig. 1(a), Bragg peaks corresponding to the tungsten bronze-like crystal structure are observed in the ceramics. And it can be indexed as a tungsten bronze structure with formulae  $BaSm_2Ti_4O_{12}$  (JCPDS Card No. 44-0062) and  $BaNd_2Ti_5O_{14}$  (JCPDS Card No. 33-0166), belonging to orthorhombic phase. All the samples doped with different amounts of  $Sr^{2+}$  ions have the same diffraction patterns. In the  $Ba(A2)Nd_2(A1)Ti_5(B)O_{14}$  solid solution, there are three kinds of cations with different ionic radii in the crystal structure. The middle-sized  $Ln^{3+}$  ions





**Fig. 1** XRD patterns of  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic specimens: (a)  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  (x=0.02, 0.04, 0.06, 0.08, 0.1) ceramics sintered at 1440 °C for 4 h; (b)  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  (x=0.08) ceramic at different sintering temperatures.

mainly occupy A1 rhombic sites, the largest Ba<sup>2+</sup> ions mainly occupy pentagonal A2 sites, and the smallest Ti<sup>4+</sup> ions alone occupy octahedral B sites [28]. The A2 sites are occupied by four Ba<sup>2+</sup> ions and A1 sites by eight Ln<sup>3+</sup> ions. Therefore, the dielectric properties of the solid solutions are highly influenced by crystal structure. Substitution of Sr<sup>2+</sup> ions (1.44 Å) for Ba<sup>2+</sup> ions (1.61 Å) in the large cation sites (A2) results in the crystal distortion, showing that the shrinkage of the TiO<sub>6</sub> octahedral site plays an important role for improvement of the microwave dielectric properties. At the same time, the distortion of the crystal lattice of the BaNd<sub>2</sub>Ti<sub>5</sub>O<sub>14</sub> phase is also expected to influence the microwave dielectric properties of the produced ceramics, which is attributed to the presence of Sr<sup>2+</sup> ions substituted for Ba<sup>2+</sup> cations. As can be seen from Fig. 1(b), with increasing sintering temperature, BaNd<sub>2</sub>Ti<sub>5</sub>O<sub>14</sub> and BaSm<sub>2</sub>Ti<sub>4</sub>O<sub>12</sub> diffraction peaks are not obviously changed, and BaNd2Ti5O14 diffraction peaks at the angles of 38°-40° are strengthened for the specimen sintered at 1440 °C.

#### 3. 2 Microstructures and density

shows the SEM micrographs  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics sintered at 1440 °C for 4 h. As can be found from the micrographs, all the samples show dense and homogeneous microstructures. Also, with the increase in the number of Sr<sup>2+</sup> ions, the pores appear in the microstructures. At the same time, an excess of Sr<sup>2+</sup> ions results in the agglomeration phenomena, preventing the better densification. On the other hand, EDX analysis was used by combining with SEM to prove that the substitution of Sr<sup>2+</sup> for Ba<sup>2+</sup> has been successfully executed, as shown in Fig. 3. It is obvious that the Sr<sup>2+</sup> ions can substitute for Ba<sup>2+</sup> ions, which is in agreement with the results of XRD patterns in Fig. 1(a). In addition, in order to understand how the Sr<sup>2+</sup> ions affect the microstructures of (Ba<sub>1-x</sub>Sr<sub>x</sub>)<sub>4</sub>(Sm<sub>0.4</sub>Nd<sub>0.6</sub>)<sub>28/3</sub>  $Ti_{18}O_{54}$  (0.02  $\leq x \leq 0.1$ ) ceramics, cross-sectional SEM micrographs are taken as shown in Fig. 4.  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  $(0.02 \le x \le 0.1)$ ceramics show agglomeration and dense and homogeneous microstructures. Furthermore, it can be clearly seen that the porosity increases with increasing x value, implying that an increase of  $Sr^{2+}$  ions ( $x \ge 0.1$ ) may deteriorate the densification of the specimens. From the observation of microstructure, the  $O \times f$  value is influenced by the defect, which results from that the

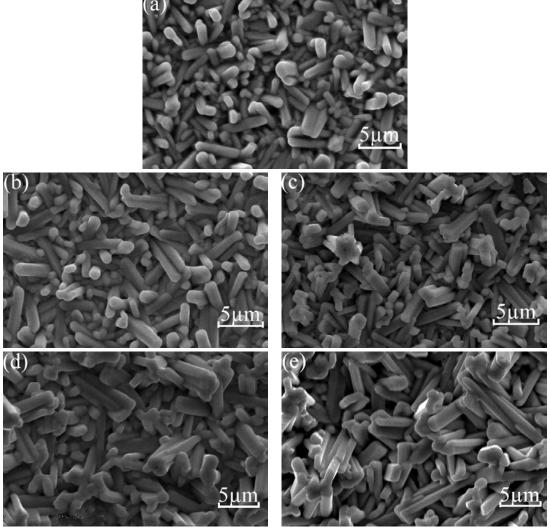
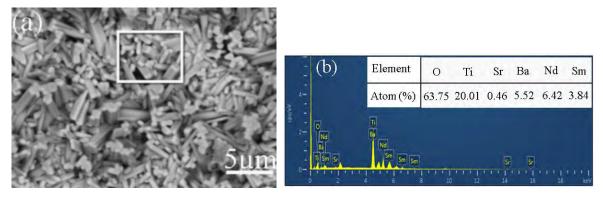


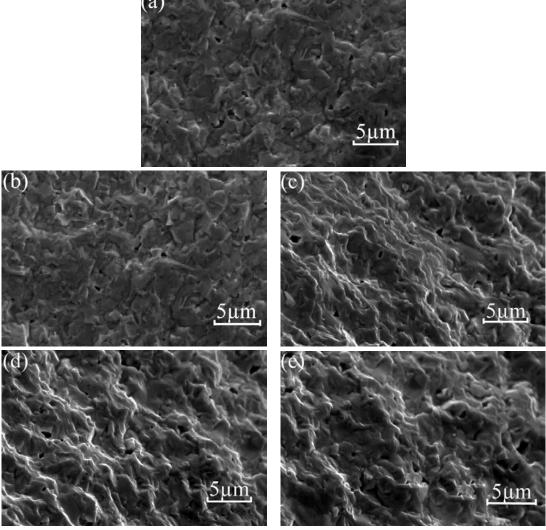
Fig. 2 SEM micrographs of  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics with (a) x = 0.02, (b) x = 0.04, (c) x = 0.06, (d) x = 0.08, and (e) x = 0.1, sintered at 1440 °C for 4 h.



**Fig. 3** EDX analysis of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic (x = 0.08) sintered at 1440 °C for 4 h.

defect can reduce the compactness of sintered ceramics and cause a decrease in  $Q \times f$  value. In addition, Fig. 5 shows the SEM images of the  $(Ba_{1-x}Sr_x)_4$   $(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic with x=0.08 sintered at different temperatures. As seen in Fig. 5, for the

composition with x=0.08, the densification degree increases with the increasing sintering temperature from 1400 to 1440 °C, and then decreases gradually when the sintering temperature is raised around 1460 °C. This phenomenon means that the degree of



**Fig. 4** SEM micrographs of the cross-section of  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics with (a) x = 0.02, (b) x = 0.04, (c) x = 0.06, (d) x = 0.08, and (e) x = 0.1, sintered at 1440 °C for 4 h.

densification at  $1440 \,^{\circ}\text{C}$  is higher than that of other sintering temperatures.

In addition, 6(a) shows the apparent density relative of and density  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  $(0.02 \le x \le 0.1)$ ceramics. As can be seen from Fig. 6(a), the increasing Sr<sup>2+</sup> content causes a reduction of the apparent density of the ceramics. At the same time, from Fig. 6(b), it is found that apparent density and relative of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$ (x = 0.08) ceramic gradually increase with the increase of sintering temperature and then obviously decrease at the further sintering temperature. Furthermore, the apparent density of  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$ (x=0.08) ceramic reaches the maximum value at 1440  $^{\circ}$ C for 4 h. The larger apparent density means the less crystal imperfection and porosity in the sample's interior structure, and a higher  $Q \times f$  value will be obtained.

#### 3. 3 Dielectric properties

Figure 7(a) shows the variation of the  $Q \times f$  value and permittivity ( $\varepsilon_r$ ) of  $(\mathrm{Ba_{1-x}Sr_x})_4(\mathrm{Sm_{0.4}Nd_{0.6}})_{28/3}\mathrm{Ti_{18}O_{54}}$  ceramics sintered at 1400 °C for 4 h. According to the literature [29], the  $Q \times f$  value and permittivity ( $\varepsilon_r$ ) of  $\mathrm{Ba_{6-3y}(Sm_{0.4}Nd_{0.6})_{8+2y}Ti_{18}O_{54}}$  (y=2/3) ceramic is ~10,700 GHz and ~82.7, respectively. As shown in Fig. 7(a), after adding  $\mathrm{Sr^{2+}}$  ions into the system, the permittivity ( $\varepsilon_r$ ) firstly increases from 90.82 to 93.19 while x value varies from 0.02 to 0.08, and then the permittivity ( $\varepsilon_r$ ) decreases to 89.76 at x=0.1. This improvement may be caused by the relaxation of local

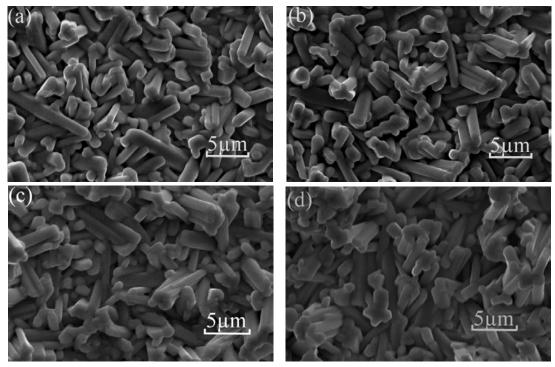
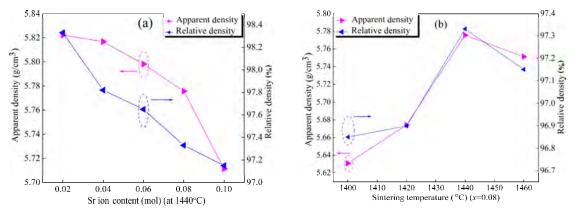


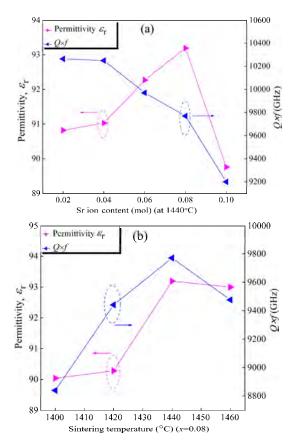
Fig. 5 SEM micrographs of  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic for x=0.08 sintered at various temperatures with (a) 1400 °C, (b) 1420 °C, (c) 1440 °C, (d) 1460 °C.



**Fig. 6** (a) Influence of the apparent density and relative density of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics on the amount of  $Sr^{2+}$  ions; (b) influence of the apparent density and relative density of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  (x=0.08) ceramic at different sintering temperatures.

distortions at A2 sites, which results from the substitution of smaller  $Sr^{2+}$  ions for  $Ba^{2+}$  ions [30]. Meanwhile, the corresponding  $Q \times f$  value slightly decreases from 10264 to 9200 GHz while x varies from 0.02 to 0.1. The dielectric relaxation caused by its large resistivity is one of the reason for the dielectric loss of  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics [31–33]. Herein, the optimal microwave dielectric properties of  $\varepsilon_r \approx 93.19$ ,  $Q \times f \approx 9770.14$  GHz (at 3.415 GHz) can be achieved at x = 0.08. The uprising of permittivity ( $\varepsilon_r$ ) with x value should be attributed to the presence of  $Sr^{2+}$  ions substituted for  $Ba^{2+}$  ions and the coexistence of

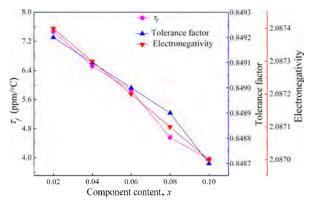
BaSm<sub>2</sub>Ti<sub>4</sub>O<sub>12</sub> and BaNd<sub>2</sub>Ti<sub>5</sub>O<sub>14</sub> phases. In addition, the  $Q \times f$  value and  $\varepsilon_r$  of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}$  Ti<sub>18</sub>O<sub>54</sub> ceramic for x=0.08 as a function of its sintering temperature for 4 h are shown in Fig. 7(b). In Fig. 7(b), the  $Q \times f$  value of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic for x=0.08 sintered at 1440 °C is relatively high due to the high density and the compact microstructure. With an increasing of sintering temperature, the  $Q \times f$  value of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic for x=0.08 increases to a maximum value of 9770.14 GHz (at 3.415 GHz) and decreases thereafter.



**Fig. 7** (a) Influence of the  $Q \times f$  value and dielectric constant ( $\varepsilon_r$ ) of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics on the amount of  $Sr^{2+}$  ions; (b) influence of the  $Q \times f$  value and dielectric constant ( $\varepsilon_r$ ) of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  (x=0.08) ceramic at different sintering temperatures.

Figure 8 shows the variation of  $\tau_f$ , electronegativity tolerance factor (e), (*t*) of  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  $(0.02 \le x \le 0.1)$ ceramics sintered at 1440 °C for 4 h. In Fig. 8, it is noted that the changes of  $\tau_f$ , electronegativity (e), and tolerance factor (t) show the same trend with the increase of x value, and the minimum values of all the parameters can be obtained at x = 0.1, which indicates that the changes of  $\tau_f$  are mainly dependent on the electronegativity (e) and tolerance factor (t) of the  $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics. Therefore, the value of  $\tau_f$  can be adjusted by  $Sr^{2+}$  ion addition with changing in the tolerance factor (t). Wherein, the tolerance factor can be calculated by the following equation:

$$t = \frac{\frac{14}{15}(0.4R_{\text{Sm}^{3+}} + 0.6R_{\text{Nd}^{3+}}) + \frac{1}{15}[(1-x)R_{\text{Ba}^{2+}} + xR_{\text{Sr}^{2+}}] + R_{\text{O}^{2-}}}{\sqrt{2}(R_{\text{Ti}^{4+}} + R_{\text{O}^{2-}})}$$



**Fig. 8** Variation of the temperature coefficient of resonant frequency ( $\tau_f$ ), electronegativity (e), and tolerance factor (t) of the (Ba<sub>1-x</sub>Sr<sub>x</sub>)<sub>4</sub>(Sm<sub>0.4</sub>Nd<sub>0.6</sub>)<sub>28/3</sub>Ti<sub>18</sub>O<sub>54</sub> ceramics with different x values sintered at 1440 °C for 4 h.

where  $R_{\rm Sm^{3+}}$ ,  $R_{\rm Nd^{3+}}$ ,  $R_{\rm Ba^{2+}}$ ,  $R_{\rm Sr^{2+}}$ ,  $R_{\rm Ti^{4+}}$ , and  $R_{\rm Q^{2-}}$  represent the ionic radii of Sm<sup>3+</sup>, Nd<sup>3+</sup>, Ba<sup>2+</sup>, Sr<sup>2+</sup>, Ti<sup>4+</sup>, and O<sup>2-</sup>, respectively [34,35]. In addition, the reduction of t illustrates that the symmetry in BaNd<sub>2</sub>Ti<sub>5</sub>O<sub>14</sub> phase has a reduction in the increase of x value. With the increase of the Sr<sup>2+</sup> ion content, the electronegativity of the tungsten bronze structure almost decreases linearly. Meanwhile, the changes of  $\tau_f$  are almost consistent with the variation of electronegativity, which also shows that the  $\tau_f$  values are strongly related with the electronegativity in tungsten bronze structure. Wherein, electronegativity (e) of the (Sm<sub>0.4</sub>Nd<sub>0.6</sub>)<sub>28/3</sub>Ti<sub>18</sub>O<sub>54</sub> solid solution can be calculated by the following equation:

$$e = \frac{4[(1-x)X_{\text{Ba-O}} + xX_{\text{Sr-O}}] + \frac{28}{3}(0.4X_{\text{Sm-O}} + 0.6X_{\text{Nd-O}}) + 18X_{\text{Ti-O}}}{32 - \frac{2}{3}}$$

where  $X_{\rm Ba-O}$ ,  $X_{\rm Sr-O}$ ,  $X_{\rm Sm-O}$ ,  $X_{\rm Nd-O}$ , and  $X_{\rm Ti-O}$  represent the electronegativity difference of  ${\rm Ba^{2^+}}$ ,  ${\rm Sr^{2^+}}$ ,  ${\rm Sm^{3^+}}$ ,  ${\rm Nd^{3^+}}$ , and  ${\rm Ti^{4^+}}$  with  ${\rm O^{2^-}}$ , respectively [36].

#### 4 Conclusions

 $(Ba_{1-x}Sr_x)_4(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  (x = 0.02, 0.04, 0.06, 0.08, 0.1) ceramics were prepared by the conventional solid-state reaction method and well densified at ~1440 °C. The phase structures, grain morphologies, and microwave dielectric properties of the  $(Ba_{1-x}Sr_x)_4$  ( $Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramics were studied. The phase structures and microwave dielectric properties were greatly influenced by x value. The optimal

(3)

microwave dielectric properties with a permittivity  $(\varepsilon_r) \approx 93.19$ , a quality factor  $(Q \times f) \approx 9770.14$  GHz (at 3.415 GHz), and an almost near-zero temperature coefficient of resonant frequency  $(\tau_f) \approx +4.56 \text{ ppm/}^{\circ}\text{C}$ can be obtained for the  $(Ba_{0.92}Sr_{0.08})_4(Sm_{0.4}Nd_{0.6})_{28/3}$ Ti<sub>18</sub>O<sub>54</sub> specimen sintered at 1440 °C for 4 h. Also, these results indicated that the (Ba<sub>0.92</sub>Sr<sub>0.08</sub>)<sub>4</sub>  $(Sm_{0.4}Nd_{0.6})_{28/3}Ti_{18}O_{54}$  ceramic with very permittivity ( $\varepsilon_r$ ), high quality factor ( $Q \times f$ ), and almost near-zero temperature coefficient of resonant frequency ( $\tau_f$ ) is a suitable candidate for microwave passive component applications.

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